

# Teaching Financial Mathematics With Plausible Reasoning 

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## APA Citation:

Hurtado, O.G., Casallas, W.P., Thiriat, W.G., (2022). Teaching Financial Mathematics With Plausible Reasoning, Journal of Language and Linguistic Studies, 18(4), 1178-1185
Submission Date: 29/10/2022
Acceptance Date: 26/12/2022


#### Abstract

This paper aims to show how through plausible reasoning financial mathematics can be taught at the university level, the work is based on a model designed by García (2019), who created it to teach linear algebra in engineering careers, using technology, of all this model, only the design with methodological procedure is adapted. In this grade The theories corresponding to money management will be developed over time, allowing you to obtain a solid foundation in the management and application of simple and compound interest in different financial applications, which will be the prerequisite to continue your studies in financial evaluation of projects. , in which he will use these tools for financial decision making. In addition, this course will implement the use of spreadsheets, to facilitate and expedite the respective calculations, thus giving the student a broad overview and useful resource for their future work performance as a professional.


Keywords: Financial mathematics, plausible reasoning, use of technology.

## 1. Introduction

This research was carried out in an engineering course at a public university and which is called economic engineering, The objective of the course is that the student is able to implement the basic tools of mathematics applied to finance, through the development of Interpretation, Argumentation and Proposition as cognitive skills, which will show their "know-how" in real situations of their work context and professional performance. To achieve this objective, the didactic proposal called teaching by plausible reasoning was chosen, since the authors already had experience in this methodological proposal, but in other subjects at the university level such as calculus and linear algebra, with very good results. Regarding plausible reasoning, Polya (1966) tells us that a mathematical theorem must be intuited before proving it, as well as the idea of proof before carrying out the details. On the other hand, Lakatos (1976) says:

## 2. Methodology.

The methodology used in this research was qualitative since it is the one that is recommended to be used in studies of educational sciences.
The population is all engineering university students who take the subject of financial mathematics or economic engineering.
The sample consisted of 30 students who were studying the Economic Engineering subject at a public university of the Faculty of Engineering in the city of Bogotá, Colombia.
In this course, the teacher implemented the methodological procedure of plausible reasoning taken from García (2019). This consists of giving some theoretical bases and through activities composed of interesting problems the student can get to build the concepts proposed by the teacher. For this, we worked in groups of three students, who developed the activities given by the teacher, the topics were compound interest, annuities and gradients.

## 3. Implementation and Results

The methodological procedure of this research is taken from García (2109) and given in the following graph:


Figure 1. Methodological procedure Source: García (2019)

### 3.1 Compound Interest.

The objective of this activity is that the student, through routine and non-routine problems with the use of technology for this work, the Excel spreadsheet, could find some laws and properties and solve the proposed problems.

Here are two problems and their respective solutions:
A Financial Entity wishes to refinance the debt to Mr. Ángelo Pulido since he has been repeatedly behind in his payments, the payment plan of Mr. Ángelo Pulido is set out as follows: Payment $\$ 600,000$ on January 30. Payment $2 \$ 1,500,000$ on February 28. Payment $3 \$ 800,000$ on August 30. If the gentleman wishes to pay in three equal installments for the last three months of the year in three equal installments, how much should the installments be if they charge him the quarterly nominal $24 \%$ in advance?

The purpose of this problem is for the student to find a relationship between money and time on different dates, that is, money loses or gains value at different times, and the interest rate must be consistent with the payment period. and lastly, to do it using technology, for this work Excel, either with the financial functions or by applying the concepts seen in class.

The solution given by a group is:


Figure 2. Solution 1
In the solution of this problem it is clearly observed how the students converted the interest rates for the required times and raised the equation that corresponded to the situation raised and then with the help of Excel to find the correct solution.

A person has the following debts: the first for $\$ 1,000,000$ acquired three months ago and maturing in four months at a rate of $20 \% \mathrm{CT}$, another for $\$ 3,000,000$ acquired today and maturing in 6 months at an effective annual rate of $20 \%$. If they allow you to refinance them for three payments of $\$ 2,000,000$ in 9 , 12 , and 15 months, what effective annual interest rate are they charging you?
The objective of this problem is for the student to make a time diagram where, by locating the payments and debts, he will find an equation that, when solved, will be the solution to the problem posed.
Solution given by a group of students:


Figure3. Solution 2
It is clearly observed that to solve this problem the students correctly made the required time-value graph and with the help of Excel, they found the indicated solution.

A person receives three offers for the purchase of his property: (a) $\$ 40,000,000$ cash; (b) $\$ 19,000,000$ cash and $\$ 5,000,000$ semi-annual, for $21 / 2$ years (c) $\$ 20,000,000$ quarterly in advance for 3 years and a
payment of $\$ 2,500,000$ at the end of the fourth year. Which offer should you choose if the interest rate is $8 \%$ per year? Baca (2000)
The purpose of the problem is that students can find a relationship between a series of uniform payments and the time in which they are made with the current and future value of money, for which two alternatives were proposed.
Solution given by a group of students:


Figure4. Solution 3
In this solution it is seen how the students clearly present the payments of each alternative and their relationship with time, then with the help of Excel they find the solution correctly.

A person has proposed to deposit $\$ 320$ monthly for 2 years ( 24 months) in a bank account that pays $18 \%$ effective annual interest. What will be the cumulative amount at the end of the two years? Baca (2000)

The purpose of the problem is for students to find a rate equivalent to that of the payments and take those payments to future value without using mathematical formulas, only with the concept and use of Excel.
Solution of a group:

| R | 320 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| i | 0,18 EA | $\sqrt[12]{1,18}-1$ | 0,0139 | EM |  |  |
| n | 24 |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  | Cuota | VF |  |  |  |  |
| 1 | 320 | 324,45 |  |  |  |  |
| 2 | 320 | 328,96 |  |  |  |  |
| 3 | 320 | 333,53 |  |  |  |  |
| 4 | 320 | 338,17 |  |  |  |  |
| 5 | 320 | 342,87 |  |  |  |  |
| 6 | 320 | 347,63 |  |  |  |  |
| 7 | 320 | 352,46 |  |  |  |  |
| 8 | 320 | 357,36 |  |  |  |  |
| 9 | 320 | 362,33 |  |  |  |  |
| 10 | 320 | 367,37 |  |  |  |  |
| 11 | 320 | 372,47 |  |  |  |  |
| 12 | 320 | 377,65 |  |  |  |  |
| 13 | 320 | 382,90 |  |  |  |  |
| 14 | 320 | 388,22 |  |  |  |  |
| 15 | 320 | 393,62 |  |  |  |  |
| 16 | 320 | 399,09 |  |  |  |  |
| 17 | 320 | 404,64 |  |  |  |  |
| 18 | 320 | 410,26 |  |  |  |  |
| 19 | 320 | 415,97 |  |  |  |  |
| 20 | 320 | 421,75 |  |  |  |  |
| 21 | 320 | 427,61 |  |  |  |  |
| 22 | 320 | 433,55 |  |  |  |  |
| 23 | 320 | 439,58 |  |  |  |  |
| 24 | 320 | 445,69 |  |  |  |  |
|  |  | 9168,14 |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| Respuesta: | La cantidad a | comulada dur | los dos | años | 9.168,14 |  |

Figure5. Solution 4
This solution clearly demonstrates that the objective of the problem was met, since the students solved it correctly as planned.

A piece of machinery will reach the end of its useful life within 2 years, by that time a new machine to be purchased will cost $\$ 9,000,000$ and it is estimated that the old machine can be received for the sum of $\$ 2,00,000$. What quarterly deposit should I make? in an account that pays $30 \%$ CM in order to be able to make the purchase at the right time if I make the first deposit at the end of 6 months? Baca (2000)

In this problem, the objective is for the student to find the value of the income in an annuity without using formulas, but only the concept and the spreadsheet.

Solution given by a group:


Figure6. Solution 5
In the solution of this problem it is clearly seen how the students raise the problem correctly and then with the help of Excel they find the payments that were required for the solution.

Determine the cash value of an asset, if financed, it is acquired as follows: an initial installment of $\$ 450,000,18$ equal monthly installments of $\$ 40,000$ each, and then quarterly installments of $\$ 150,000$ the first, $\$ 160,000$ the second, $\$ 170,000$ the third, and so on until the end of the fourth year; finally six months after the last of these quarterly installments, a payment equivalent to $15 \%$ of the cash value. The interest rate is $36 \%$ per year. RTA: $\$ 1888380$.

The objective of this problem is for the student to relate a series of payments with linear growth over time in a specific focal coot.

Solution given by a group of students:

| 0 | 450000 | 450000 | 45000 |  |  |  | 544216 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 40000 | 40000 | 4000 |  |  |  |  |  |  |
| 2 | 40000 | 38988,0711 | 41038,193 |  |  |  |  |  |  |
| 3 | 40000 | 38001,7421 | 42103,332 |  |  |  | 136279,863 |  |  |
| 4 | 40000 | 37040,3656 | 43196,11 |  |  |  |  |  |  |
| 5 | 40000 | 36103,3101 | 44317,266 |  |  |  |  |  |  |
| 6 | 40000 | 35189,9605 | 45467,513 |  |  |  |  |  |  |
| 7 | 40000 | 34299,717 | 46647,615 |  |  |  |  |  |  |
| 8 | 40000 | 33431,9951 | 47858,346 |  |  |  |  |  |  |
| 9 | 40000 | 32586,225 | 49100,501 |  |  |  |  |  |  |
| 10 | 40000 | 31761,8514 | 50374,897 |  |  |  |  |  |  |
| 11 | 40000 | 30958,333 | 51682,369 |  |  | 36\% | 0,36000 | EA |  |
| 12 | 40000 | 30175,1422 | 53023,776 |  |  | 8\% | 0,07990 | ET |  |
| 13 | 40000 | 29411,7647 | 5440 |  |  | 3\% | 0,02595 | EM |  |
| 14 | 40000 | 28667,6993 | 55811,94 |  |  | 15\% |  |  |  |
| 15 | 40000 | 27942,4574 | 57260,532 |  |  |  |  |  |  |
| 16 | 40000 | 27235,5629 | 58746,720 |  |  |  |  |  |  |
| 17 | 40000 | 26546,5516 | 60271,481 |  |  |  |  |  |  |
| 18 | 40000 | 25874,971 | 61835,818 |  |  |  |  |  |  |
| 19 |  |  |  |  |  |  |  |  |  |
| 20 |  |  |  |  |  |  |  |  |  |
| 21 | 150000 | 75098,0595 | 349400,28 |  |  |  |  |  |  |
| 22 |  | 0 |  |  |  |  |  |  |  |
| 23 |  | 0 |  |  |  |  |  |  |  |
| 24 | 160000 | 63606,7576 | 469360,09 |  |  |  |  |  |  |
| 25 |  | 0 |  |  |  |  |  |  |  |
| 26 |  | 0 |  |  |  |  |  |  |  |
| 27 | 170000 | 53663,379 | 628042,85 |  |  |  |  |  |  |
| 28 |  | 0 |  |  |  |  |  |  |  |
| 29 |  | 0 |  |  |  |  |  |  |  |
| 30 | 180000 | 45117,7483 | 837465,73 |  |  |  |  |  |  |
| 31 |  | 0 |  |  |  |  |  |  |  |
| 32 |  | 0 |  |  |  |  |  |  |  |
| 33 | 190000 | 37815,8905 | 1113274,6 |  |  |  |  |  |  |
| 34 |  | 0 |  |  |  |  |  |  |  |
|  |  | 35 |  | 0 |  |  |  |  |  |
|  |  | 36 | 200000 | 31607,9657 | 1475818,33 |  |  |  |  |
|  |  | 37 |  | 0 |  |  |  |  |  |
|  |  | 38 |  | 0 |  |  |  |  |  |
|  |  | 39 | 210000 | 26353,0972 | 1951535,16 |  |  |  |  |
|  |  | 40 |  | 0 |  |  |  |  |  |
|  |  | 41 |  | 0 |  |  |  |  |  |
|  |  | 42 | 220000 | 21922,0351 | 2574743,37 |  |  |  |  |
|  |  | 43 |  |  |  |  |  |  |  |
|  |  | 44 |  |  |  |  |  |  |  |
|  |  | 45 |  |  |  |  |  |  |  |
|  |  | 46 |  |  |  |  |  |  |  |
|  |  | 47 |  |  |  |  |  |  |  |
|  |  | 48 | 67500 | 67500 | 67500 |  |  |  |  |

Figure7. Solution6

It is observed that the students raise the payments correctly and solve the problem with the help of Excel, correctly finding the socuón.

Suppose that we currently have 10 million pesos to invest. One possibility is to create a company that, according to marketing studies, is estimated to yield annual profits of $\$ 2,549,000$ for 10 years with zero salvage value at the end of this time. We want to know what is the profitability of the project of creating
this company. On the other hand, we also have the opportunity to invest the 10 million pesos in a banking institution that offers us an interest rateof $21 \%$ per year.
The purpose of this problem is that the student can choose the best option of two financing alternatives for a given project.
Solution given by a group of students

|  | Ingresos | Egresos |  | 0,22000607 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 |  | 10000000 | -10000000 |  |  | 0 | 10000000 |  |  |  |
| 1 | 2549000 |  | 2089333,87 | 2549000 |  | 1 | 10000000 | 10000000 |  |  |
| 2 | 2549000 |  | 1712560,22 | 3109795,472 |  | 2 | 10000000 | 12100000 |  |  |
| 3 | 2549000 |  | 1403730,9 | 3793969,353 |  | 3 | 12100000 | 17715610 |  |  |
| 4 | 2549000 |  | 1150593,38 | 4628665,64 |  | 4 | 17715610 | 31384283,77 |  |  |
| 5 | 2549000 |  | 943104,633 | 5647000,176 |  | 5 | 31384283,8 | 67274999,49 |  |  |
| 6 | 2549000 |  | 773032,738 | 6889374,493 |  | 6 | 67274999,5 | 174494022,7 |  |  |
| 7 | 2549000 |  | 633630,239 | 8405078,699 |  | 7 | 174494023 | 547636992,4 |  |  |
| 8 | 2549000 |  | 519366,464 | 10254247,03 |  | 8 | 547636992 | 2079650567 |  |  |
| 9 | 2549000 |  | 425708,099 | 12510243,62 |  | 9 | 2079650567 | 9555938177 |  |  |
| 10 | 2549000 |  | 348939,328 | 15262573,16 |  | 10 | 9555938177 | 53130226118 |  |  |
|  |  |  | -0,12885567 | \$ 73.049.948 | Empresa |  |  | \$ 53.120.226.118 | Banco |  |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | -\$73.049.947,64 |  |  |  |  |  |  |

Figure8. Solution7

It is clearly observed how the students correctly raise the two alternatives and through correct calculations using the spreadsheet they arrive at the best alternative alternative.

## 4. Conclusions

The research showed that, by applying a set of activities based on a didactic procedure focused on plausible reasoning and the use of technology to solve financial mathematics problems, learning in this subject in engineering careers is significantly improved. Not onlyin conjectures but also in deductions of basic properties of the theory of interest to students. This affirmation is supported by the results of the solutions of the problems carried out by the students.
Attention was paid to the tendencies of the students when developing these activities in the search for arguments that would allow them to conjecture or justify results, without being tied to algorithmic procedures in a mechanical way.
From what was observed in the study, it can be concluded that the use of technology should be used in practices for the development of the programmatic contents of the subject in engineering careers.

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